# Bisecting Beat Speed Windows Temperament Sequences <br> For Accurate Bass and Treble Stretch 

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## Tuning Octaves Above the Temperament

F\#4 to B4, as pure or wide 4:2, using and confirming a P 4 window

| Tune | P4 Window | Pure/Wide 4:2 and <br> Wide P4 Tests | Beating <br> Partials |
| :---: | :---: | :---: | :---: |
| F\#4 | D3F\#3<D3B3 | D3F\#3 <= D3F\#4 < D3B3 | F\#5 |
| G4 | D\#3G3<D\#3C4 | D\#3G3 $<=$ D\#G4 $<$ D\#3C4 | G5 |
| G\#4 | E3G\#3<E3C\#4 | E3G\#3 $<=$ E3G\#4 $<$ E3C\#4 | G\#5 |
| A4 |  | A4 TUNED ALREADY |  |
| A\#4 | F\#3A\#3<F\#3D\#4 | F\#3A\#3 $<=$ F\#3A\#4 $<$ F\#3D\#4 | A\#5 |
| B4 | G3B3<G3E4 | G3B3 $<=$ G3B4 $<$ G3E4 | B5 |

Try for wide 4:2 if the octaves were medium scale.

## Tuning Octaves Above the Temperament

C5 to E5, as pure 12th and using and confirming a P5 window.

| Tune | P5 Window | Pure P12, Narrow P5 Tests | Beating <br> Partials |
| :---: | :---: | :---: | :---: |
| C5 | G\#2F3 $>$ G\#2C4 | G\#2F3 $=$ G\#2C5 $>$ G\#2C4 | C5 |
| C\#5 | A2F\#3 $>$ A2C\#4 | A2F\#3 $=$ A2C\#5 $>$ A2C\#4 | C\#5 |
| D5 | A\#2G3 > A\#2D4 | A\#2G3 $=$ A\#2D5 $>$ A\#2D4 | D5 |
| D\#5 | B2G\#3 > B2D\#4 | B2G\#3 $=$ B2D\#5 $>$ B2D\#4 | D\#5 |
| E5 | C3A3 > C3E4 | C3A3 $=$ C3E5 $>$ C3E4 | E5 |

## Tuning Octaves Above the Temperament

F5 to E6, as pure 12ths and confirming a pure/wide 4:2 and a wide 2:1, using and confirming a P4 window

| Tune | P4 Window | Pure/Wide 4:2, Wide 2:1, Pure P12 Tests | Beating Partial |
| :---: | :---: | :---: | :---: |
| F5 | C\#3F3<C\#3A\#3 | C\#3F3 <= C\#3F4 < C\#3F5 = C\#3A\#3 | F5 |
| F\#5 | D3F\#3<D3B3 | D3F\#3 <= D3F\#4 < D3F\#5 = D3B3 | F\#5 |
| G5 | D\#3G3<D\#3C4 | D\#3G3 <= D\#3G4 < D\#3G5 = D\#3C4 | G5 |
| G\#5 | E3G\#3<E3C\#4 | E3G\#3 <= E3G\#4 < E3G\#5 = E3C\#4 | G\#5 |
| A5 | F3A3<F3D4 | F3A3 $<=$ F3A4 $<$ F3A5 = F3D4 | A5 |
| A\#5 | F\#3A\#3<F\#3D\#4 | F\#3A\#3 <= F\#3A\#4 < F\#3A\#5 = F\#3D\#4 | A\#5 |
| B5 | G3B3<G3E4 | G3B3 <= G3B4 < G3B5 = G3E4 | B5 |
| C6 | G\#3C4<G\#3F4 | G\#3C4 <= G\#3C5 < G\#3C6 = G\#3F4 | C6 |
| C\#6 | A3C\#4<A3F\#4 | A3C\#4 <= A3C\#5 < A3C\#6 = A3F\#4 | C\#6 |
| D6 | A\#3D4<A\#3G4 | A\#3D4 <= A\#3D5 < A\#3D6 = A\#3G4 | D6 |
| D\#6 | B3D\#4<B3G\#4 | B3D\#4 <= B3D\#5 < B3D\#6 = B3G\#4 | D\#6 |
| E6 | C4E4<C4A4 | C4E4 <= C4E5 < C4E6 = C4A4 | E6 |

## Tuning Octaves Above the Temperament

F6 to B6, as pure 22nds and pure 12ths, confirming a pure/wide 4:2 and a wide 2:1, using and confirming a $8: 4$ window.

| Tune | 8:4 Window | Pure/Wide 4:2, Wide 2:1, Pure P12, Pure 22nd Tests | Beating Partial |
| :---: | :---: | :---: | :---: |
| F6 | C\#4F4<F3C\#4 | C\#4F4 < C C 4F5 < C\#4F6 = C\#4A\#4 = F3C\#4 | F6 |
| F\#6 | D4F\#4<F\#3D4 | D4F\#4 <= D4F\#5 < D4F\#6 = D4B4 = F\#3D4 | F\#6 |
| G6 | D\#4G4<G3D\#4 | D\#4G4 <= D\#4G5 < D\#4G6 = D\#4C5 = G3D\#4 | G6 |
| G\#6 | E4G\#4<G\#3E4 | E4G\#4 <= E4G\#5 < E4G\#6 = E4C\#5 = G\#3E4 | G\#6 |
| A6 | F4A4<A3F4 | F4A4 <= F4A5 < F4A6 $=$ F4D5 $=$ A3F4 | A6 |
| A\#6 | F\#4A\#4<A\#3F\#4 | F\#4A\#4 <= F\#4A\#5 $<$ F\#4A\#6 $=$ F\#4D\#5 $=$ A\#3F\#4 | A\#6 |
| B6 | G4B4<B3G4 | $\mathrm{G} 4 \mathrm{~B} 4<=\mathrm{G} 4 \mathrm{~B} 5<\mathrm{G} 4 \mathrm{~B} 6=\mathrm{G} 4 \mathrm{E} 5=\mathrm{B} 3 \mathrm{G} 4$ | B6 |

Tuning Octaves Above the Temperament C7 to C8, as pure 22nds and pure 12ths, listening directly, i.e. no check notes.

| Tune | Pure 12th | Pure 22nd | Beating <br> Partial |
| :---: | :---: | :---: | :---: |
| C7 | F5C7 | C4C7 | C7 |
| C\#7 | F\#5C\#7 | C\#4C\#7 | C\#7 |
| D7 | G5D7 | D4D7 | D7 |
| D\#7 | G\#5D\#7 | D\#4D\#7 | D\#7 |
| E7 | A5E7 | E4E7 | E7 |
| F7 | A\#5F7 | F4F7 | F7 |
| F\#7 | B5F\#7 | F\#4F\#7 | F\#7 |
| G7 | C6G7 | G4G7 | G7 |
| G\#7 | C\#6G\#7 | G\#4G\#7 | G\#7 |
| A7 | D6A7 | A4A7 | A7 |
| A\#7 | D\#6A\#7 | A\#4A\#7 | A\#7 |
| B7 | E6B7 | B4B7 | B7 |
| C8 | F6C8 | C5C8 | C8 |
| Yan |  |  |  |

You can also use the octave below to get close.

## Tuning Octaves Below the Temperament

 E3 to lowest bichord, as pure 22nds, confirming pure/wide 4:2's. wide 2:1's and pure P12's, using an 8:4 window.| Tune | 8:4 Window | Pure/Wide 4:2, Wide 2:1, <br> Pure P12, Pure 22nd Tests | Beating <br> Partial |
| :---: | :---: | :---: | :---: |
| E3 | E3C4>C4E4 | C4E4 $<=$ C4E5 $<$ C4E6 $=$ C4A4 $=$ E3C4 | E6 |
| D\#3 | D\#3B3>B3D\#4 | B3D\#4 $<=$ B3D\#5 $<$ B3D\#6 $=$ B3G\#4 $=$ D\#3B3 | D\#6 |
| D3 | D3A\#3>A\#3D4 | A\#3D4 $<=$ A\#3D5 $<$ A\#3D6 $=$ A\#3G4 $=$ D3A\#3 | D6 |
| C\#3 | C\#3A3>A3C\#4 | A3C\#4 $<=$ A3C\#5 $<$ A3C\#6 $=$ A3F\#4 $=$ C\#3A3 | C\#6 |
| C3 | C3G\#3>G\#3C4 | G\#3C4 $<=$ G\#3C5 $<$ G\#3C6 $=$ G\#3F4 $=$ C3G\#3 | C5 |
| B2 | B2G3>G3B3 | G3B3 $<=$ G3B4 $<$ G3B5 $=$ G3E4 $=$ B2G3 | B5 |
| A\#2 | A\#2F\#3>F\#3A\#3 | F\#3A\#3 $<=$ F\#3A\#4 $<$ F\#3A\#5 $=$ F\#3D\#4 $=$ A\#2F\#3 | A\#5 |
| A2 | A2F3>F3A3 | F3A3 $<=$ F3A4 $<$ F3A5 $=$ F3D4 $=$ A2F3 | A5 |
| G\#2 | G\#2E3>E3G\#3 | E3G\#3 $<=$ E3G\#4 $<$ E3G\#5 $=$ E3C\#4 $=$ G\#2E3 | G\#5 |
| G2 | G2D\#3>D\#3G3 | D\#3G3 $<=$ D\#3G4 $<$ D\#3G5 $=$ D\#3C4 $=$ G2D\#3 | G5 |
| F\#2 | F\#2D3>D3F\#3 | D3F\#3 $<=$ D3F\#4 $<$ D3F\#5 $=$ D3B3 $=$ F\#2D3 | F\#5 |
| F2 | F2C\#3>C\#3F3 | C\#3F3 $<=$ C\#3F4 $<$ C\#3F5 $=$ C\#3A\#3 $=$ F2C\#3 | F5 |

## Tuning Octaves Below the Temperament

 E3 to lowest bichord, as pure 22nds, confirming pure/wide 4:2's. wide 2:1's and pure P12's, using an 8:4 window.| Tune | 8:4 Window | Pure/Wide 4:2, Wide 2:1, Pure P12, Pure 22nd Tests | Beating Partial |
| :---: | :---: | :---: | :---: |
| E2 | E2C3>C3E3 | C3E3 <= C3E $4<\mathrm{C} 3 \mathrm{E} 5=\mathrm{C} 3 \mathrm{~A} 3=\mathrm{E} 2 \mathrm{C} 3$ | E6 |
| D\#2 | D\#2B2>B2D\#3 | B2D\#3 <= B2D\#4 < B2D\#5 = B2G\#3 = D\#2B2 | D\#6 |
| D2 | D2A\#2>A\#2D3 | A\#2D3 <= A\#2D4 < A\#2D5 = A\#2G3 = D2A\#2 | D6 |
| C\#2 | C\#2A2>A2C\#3 | A2C\#3 <= A2C\#4 < A2C\#5 = A2F\#3 = C\#2A2 | C\#6 |
| C2 | C2G\#2>G\#2C3 | G\#2C3 <= G\#2C4 < G\#2C5 = G\#2F3 = C2G\#2 | C5 |
| B1 | B1G2>G2B2 | G2B2 <= G2B3 < G2B4 = G2E3 = B1G2 | B5 |
| A\#1 | A\#1F\#2>F\#2A\#2 | F\#2A\#2 <= F\#2A\#3 < F\#2A\#4 = F\#2D\#3 = A\#1F\#2 | A\#5 |
| A1 | A1F2>F2A2 | F2A2 < F 2 A3 < F2A4 $=$ F2D3 = A1F2 | A5 |
| G\#1 | G\#1E2>E2G\#2 | E2G\#2 <= E2G\#3 < E2G\#4 = E2C\#3 = G\#1E2 | G\#5 |
| G1 | G1D\#2>D\#2G2 | D\#2G2 <= D\#2G3 < D\#2G4 = D\#2C3 = G1D\#2 | G5 |
| F\#1 | F\#1D2>D2F\#2 | D2F\#2 <= D2F\#3 < D2F\#4 = D2B2 = F\#1D2 | F\#5 |
| F1 | F1C\#2>C\#2F2 | C\#2F2 < C C 2F3 < C\#2F4 = C\#2A\#2 = F1C\#2 | F5 |

## Tuning Octaves Below the Temperament

Lowest bichord to A0, as a clean octave, listening to the whole sound and the natural beat at the bottom note.

| Tune | From | Listening at |
| :---: | :---: | :---: |
| E1 | E2 | E1 |
| D\#1 | D\#2 | D\#1 |
| D1 | D2 | D1 |
| C\#1 | C\#2 | C\#1 |
| C1 | C2 | C1 |
| B0 | B1 | B0 |
| A\#0 | A\#1 | A\#0 |
| A0 | A1 | A0 |

## Notes on the Low Octaves

1. The lower the octave and the shorter the strings, the harder it will be to get a clean sound.
2. Sometimes the windows will be hard to hear for the lowest bichords. In these cases, tune the natural beat* clean.
*The natural beat is a perceived beat occurring at the lowest note.
